

Dynamics of Liquid-Filled Spacecraft

Numerical Simulation of Coupled Solid-Liquid Dynamics

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The cover shows an artist impression, created by the Graphic Design Group of the Dutch National Aerospace Laboratory NLR, of the experiment satellite SloshSat FLEVO flying in space.

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